
9TH

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Risk and Uncertainty in Engineering Computations

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Hysteretic Tuned Mass Dampers for Seismic Protection

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Tuned Mass Damper

A **Tuned Mass Damper (TMD)** is a device that is attached to the main system in order to reduce the dynamic response that the latter exhibits when exposed to external excitations.

TMD Classification:

- Active
- Semi-active
- Hybrid
- **Passive**
 - **Conventional TMD**
 - Pendulum TMD
 - Tuned Liquid Damper



Taipei World Financial
Center, Taiwan



Towards the seismic application

Despite the fact that TMDs are recognized as effective devices to mitigate wind-induced vibrations, their seismic effectiveness still remains an open issue.

Open challenges:

- **Detuning**

(Wong KKF, Harris JL, 2012)

- **Impulsive loading**

(Sladek, John R., and Richard E. Klingner, 1983)

- **Higher vibration modes**

- **Lack of experimentation**



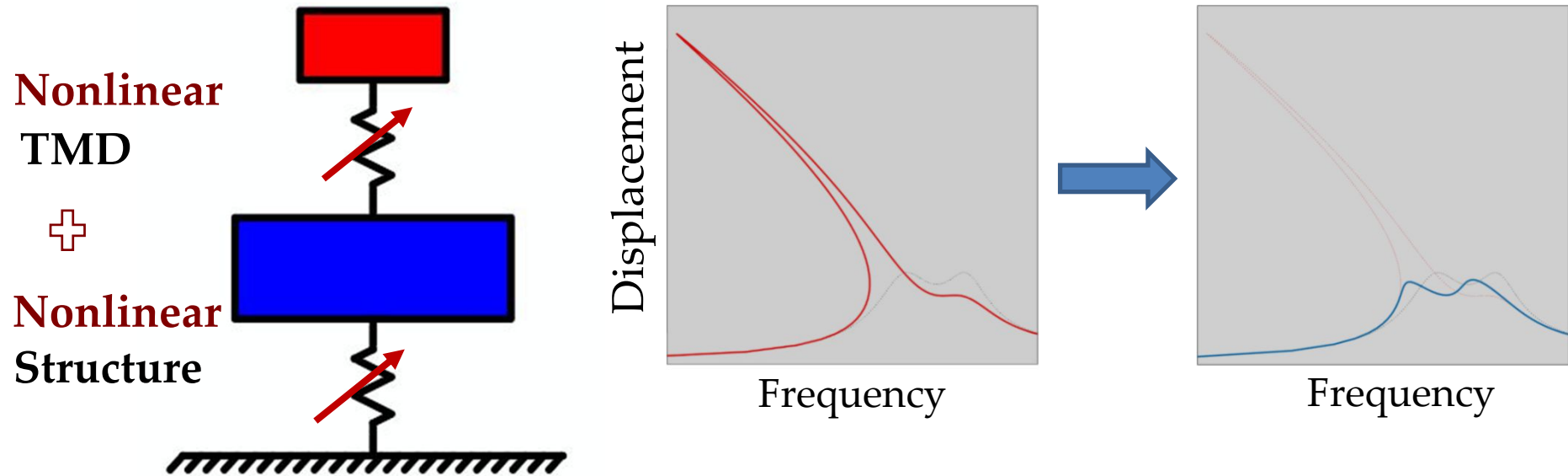
LAX Theme Building



Berlin TV Tower



Detuning Effect



Innovative aspect of the work :

- taken into account, at the same time, the **nonlinear behaviour of the structures** to be controlled and the **nonlinear behaviour of the vibration absorber**;
- **new identification and optimization strategies** proposed.



Mechanical Model

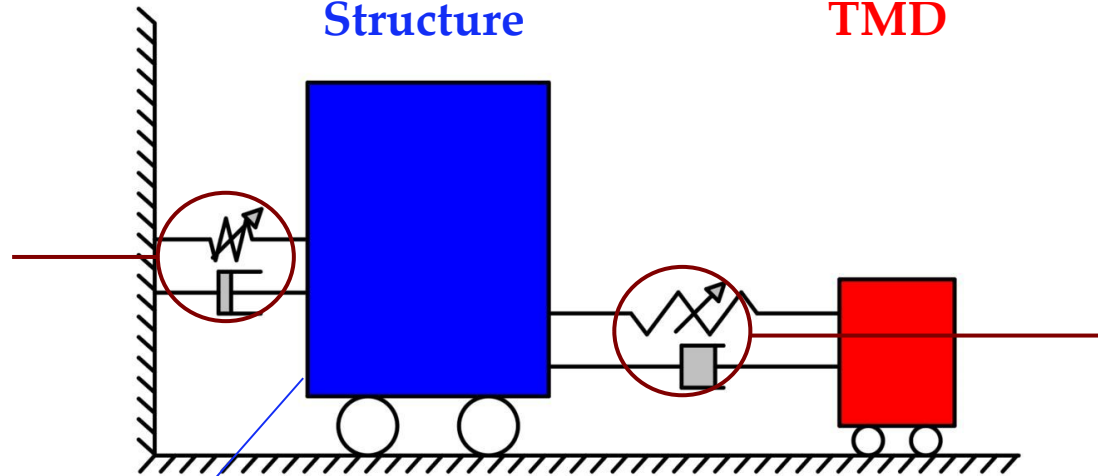
2-DOFs System

Bouc-Wen
Model

Identification

Structure

TMD

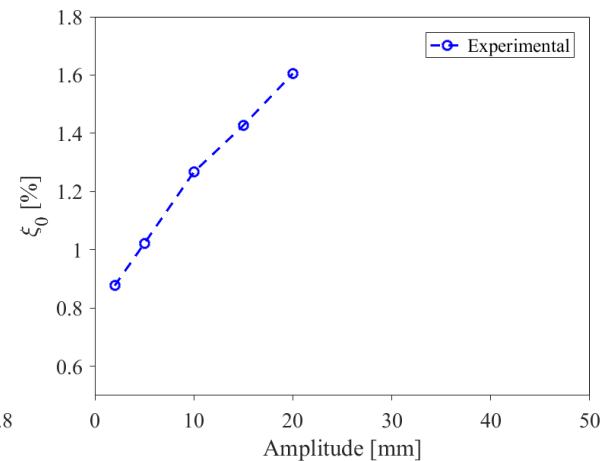
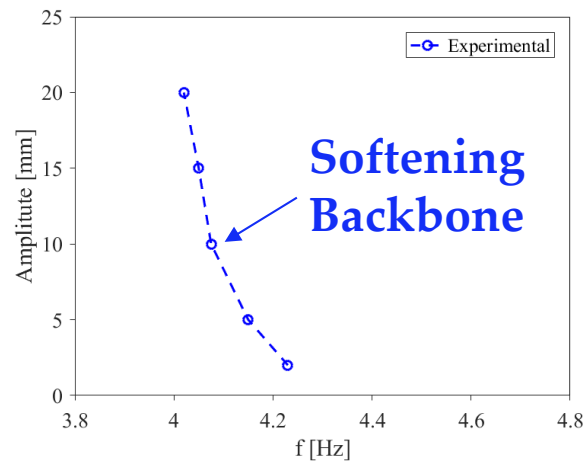


Modified
Bouc-Wen
Model
and Cubic
stiffness

Optimization

$$\theta = \{k_{e1}, k_{d1}, \gamma_1, \beta_1, n_1\}$$

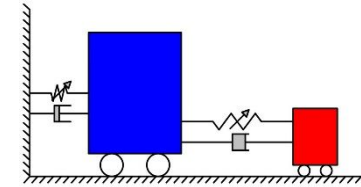
$$\mathbf{d} = \{k_{e2}, k_{d2}, \gamma_2, \beta_2, n_2, m_2, \xi_H, x_H\}$$



Carboni B. and
W. Lacarbonara.
*Journal of
Engineering
Mechanics* 142.5
(2016): 04016023.



The BW model of hysteresis



Structure: Bouc-Wen Model

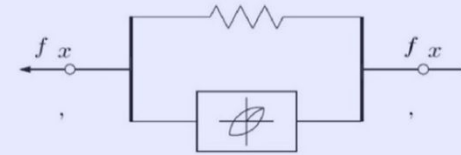
$$f(t) = k_e x + z$$

$$\dot{z} = \{k_d - [\gamma + \beta \operatorname{sgn}(z\dot{x})]|z|^n\} \dot{x}$$

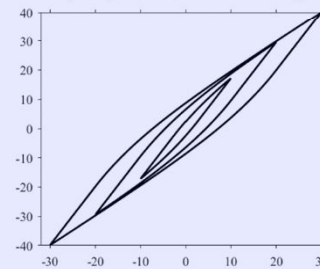
where $\gamma, \beta \in R, n \in R^+$

Softening/hardening
behaviour

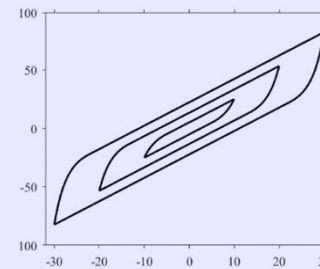
Smoothness
transition



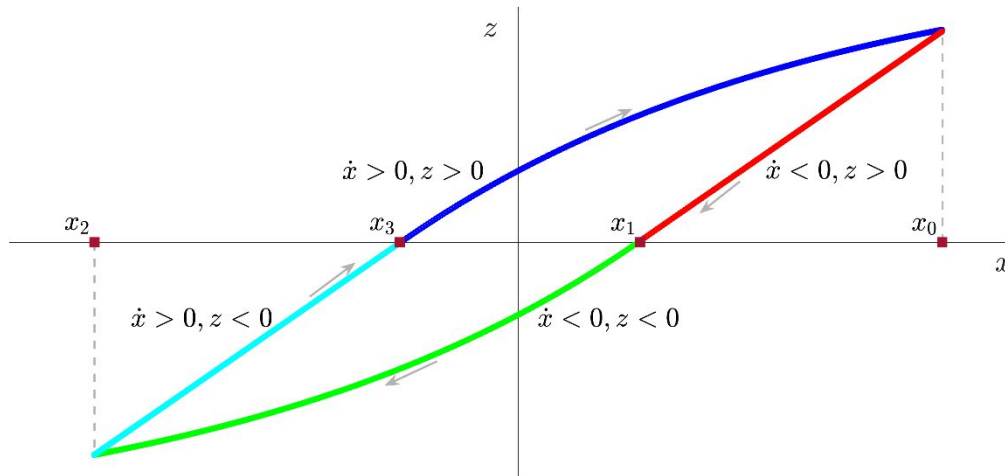
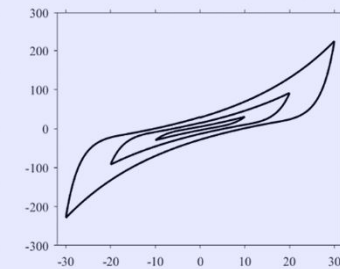
$\gamma + \beta > 0$ softening



$\gamma + \beta = 0$ quasi-linear



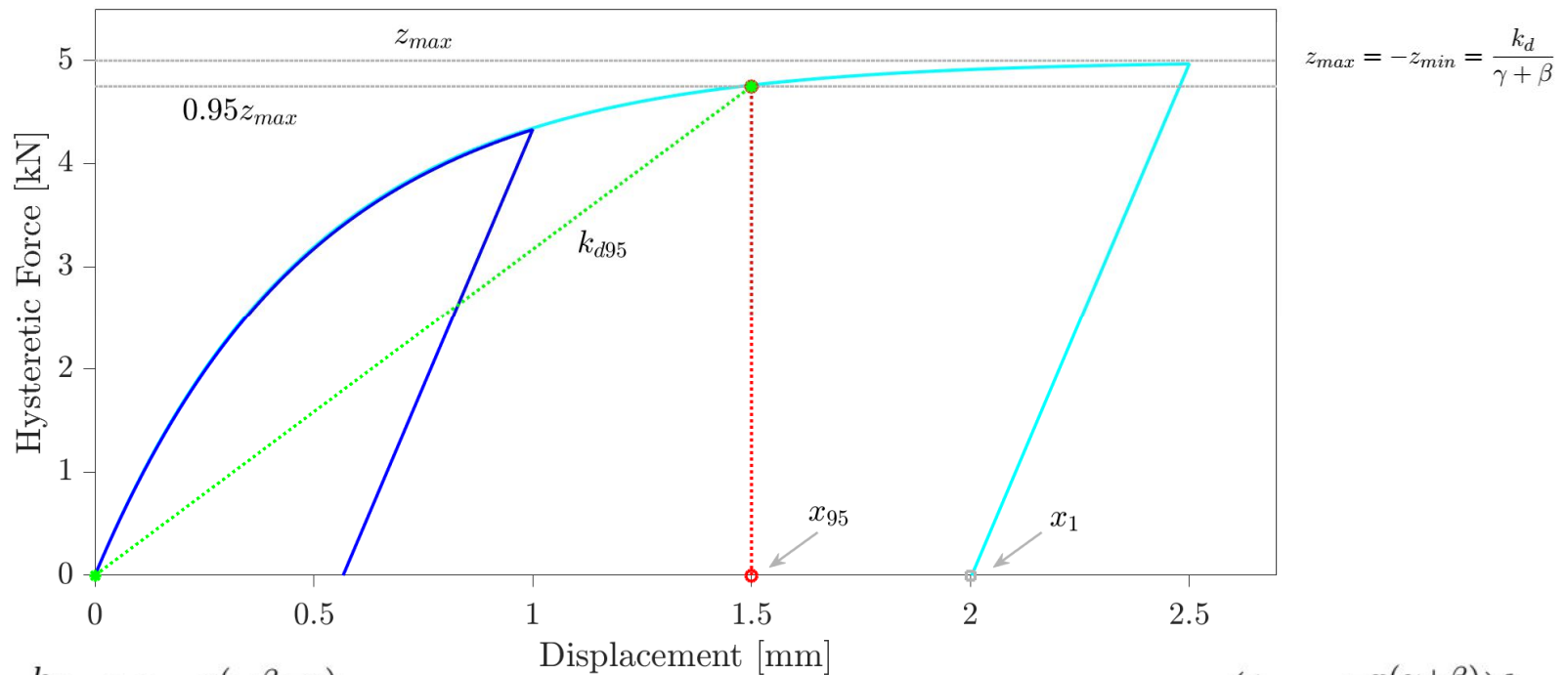
$\gamma + \beta < 0$ hardening



Branch	z	\dot{x}	z_x	z
1	> 0	< 0	$k_d + (\gamma - \beta)z$	$\frac{k_d}{\gamma - \beta} + b_1 e^{x(\beta - \gamma)}$
2	< 0	< 0	$k_d - (\gamma + \beta)z$	$-\frac{k_d}{\gamma + \beta} + b_2 e^{x(\beta + \gamma)}$
3	> 0	< 0	$k_d - (\gamma - \beta)z$	$\frac{k_d}{-\gamma + \beta} + b_3 e^{x(-\beta + \gamma)}$
4	> 0	> 0	$k_d + (\gamma + \beta)z$	$\frac{k_d}{\gamma + \beta} + b_4 e^{x(-\beta - \gamma)}$



The BW model of hysteresis



$$z_{fl}(x) = \frac{k_d}{\gamma + \beta} + b_4 e^{x(-\beta - \gamma)} \quad \rightarrow \quad b_4 = -\frac{k_d}{\gamma + \beta} \quad \rightarrow \quad z_{fl}(x) = \frac{(1 - e^{-x(\gamma + \beta)})k_d}{\gamma + \beta}$$

$$z(0) = 0$$

$$z(x_{95}) = 0.95 z_{max} \quad \rightarrow \quad x_{95} = \frac{-\ln(0.05)}{\gamma + \beta} \simeq \frac{3}{\gamma + \beta}$$

$$k_{d95} = \frac{0.95 z_{max}}{x_{95}} = \frac{0.95 k_d}{-\ln(0.05)} \simeq 0.317 k_d$$



The hysteretic oscillator

$$m\ddot{x} + f(x) = -m\ddot{x}_g$$

$$f(x) = k_e x + z(x)$$

$$\dot{z} = \{k_d - [\gamma + \beta \operatorname{sgn}(\dot{x}z)]|z|^n\}\dot{x}$$

$$m = 1 \text{ kg}$$

$$k_e = 10 \text{ N/m}$$

$$k_d = 30 \text{ N/m}$$

$$\gamma = \beta = 0.5 \text{ mm}^{-1}$$

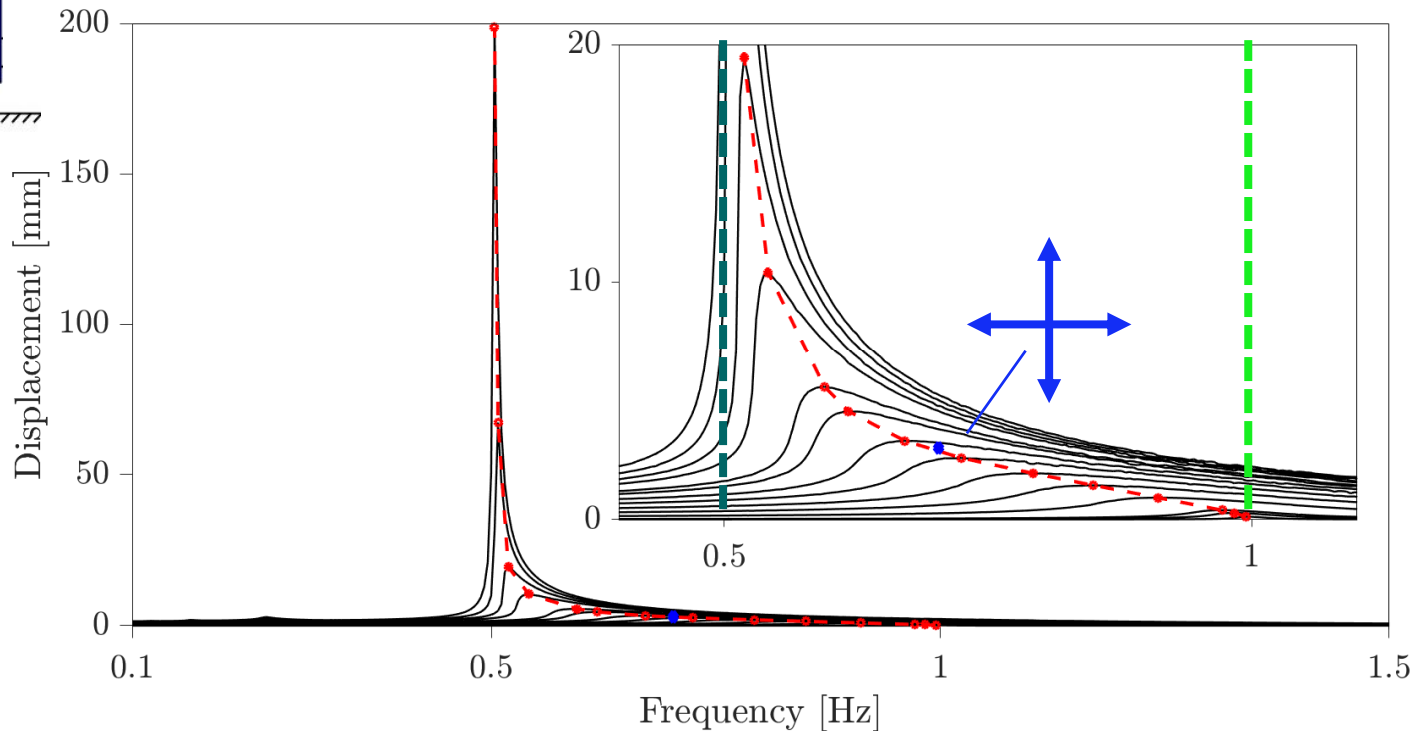
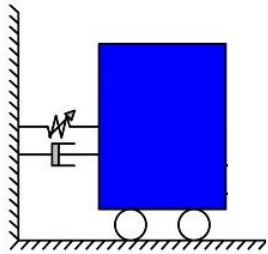
$$n = 1$$

$$f_{ul} = \frac{1}{2\pi} \sqrt{\frac{k_e}{m}} = 1.00 \text{ Hz}$$

$$f_{in} = \frac{1}{2\pi} \sqrt{\frac{k_e + k_d}{m}} = 0.50 \text{ Hz}$$

$$f_{95} = \frac{1}{2\pi} \sqrt{\frac{k_e + 0.317k_d}{m}} = 0.70 \text{ Hz}$$

$$x_{95} = \frac{3}{\gamma + \beta} = 3.00 \text{ mm}$$

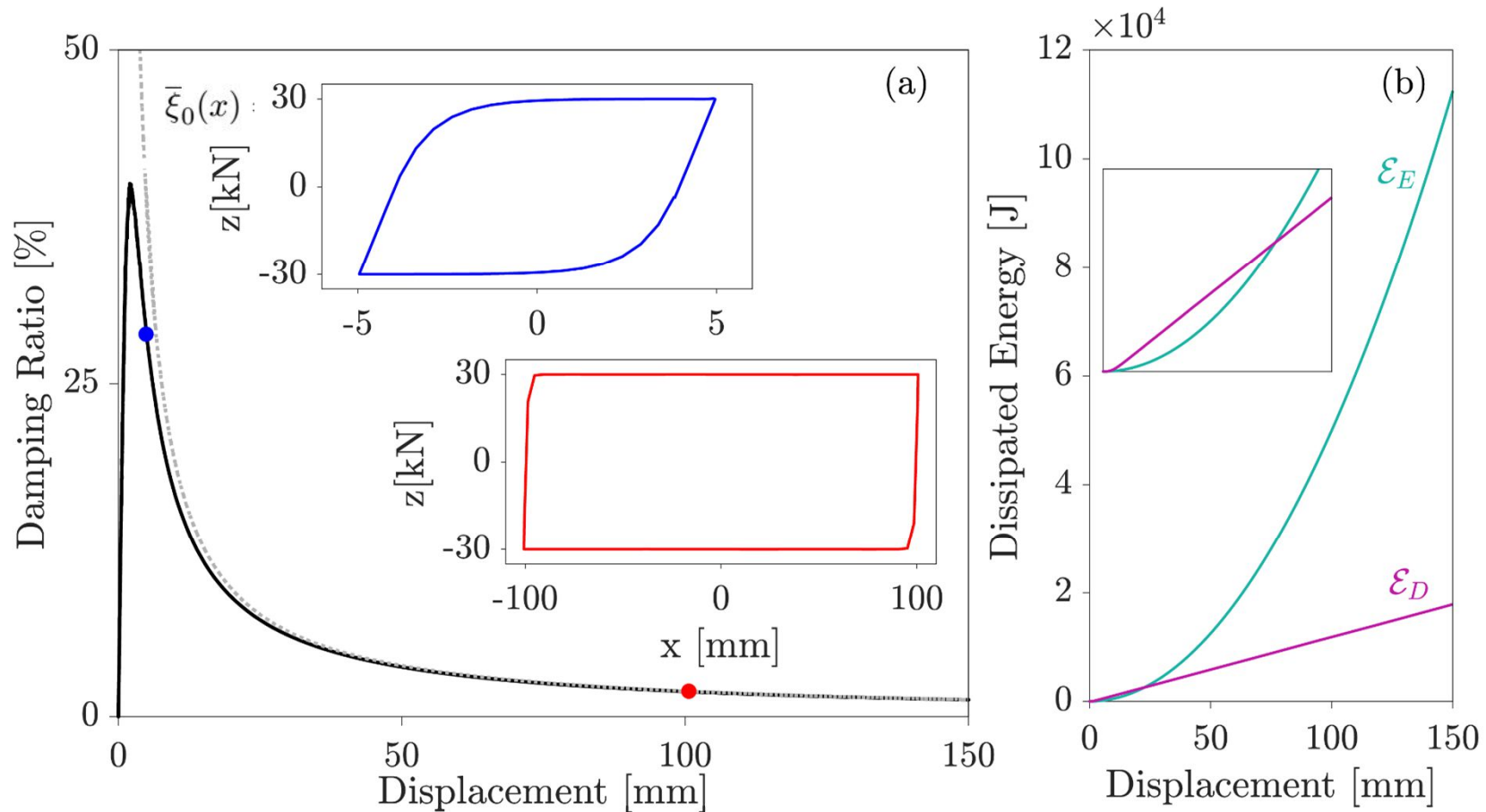




The hysteretic oscillator

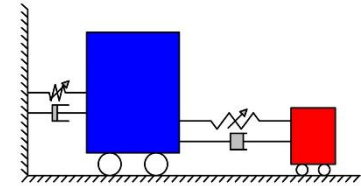
$$\xi_0 = \frac{\mathcal{E}_D}{4\pi \mathcal{E}_E}$$

● $\mathcal{E}_E = \frac{1}{2} k_e x_0^2$
● $\mathcal{E}_D = \int_{-x_0}^{x_0} z dx \simeq 4 z_{max} x_0$
● $\bar{\xi}_0(x) = \frac{2 k_d}{k_e \pi (\gamma + \beta) x}$





The modified BW model of hysteresis



TMD: Modified Bouc-Wen Model

$$\dot{z} = \{k_d H(x) - [\gamma + \beta \operatorname{sgn}(z\dot{x})]|z|^n\} \dot{x}$$

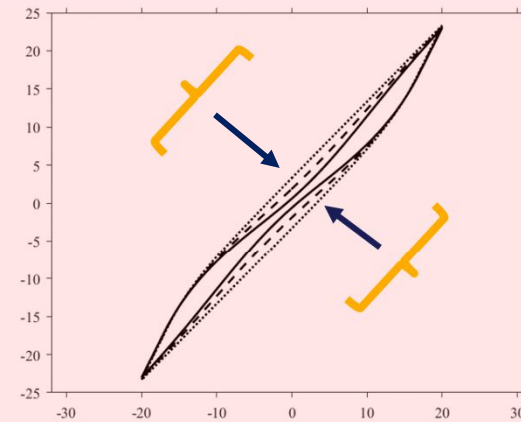
$$H(x) = 1 - \xi_0 e^{-\frac{x^2}{x_0}}$$

Pinching function

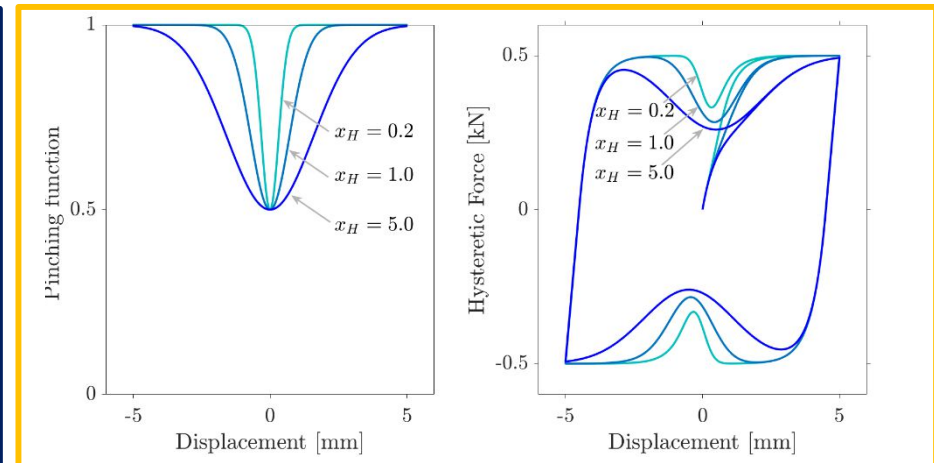
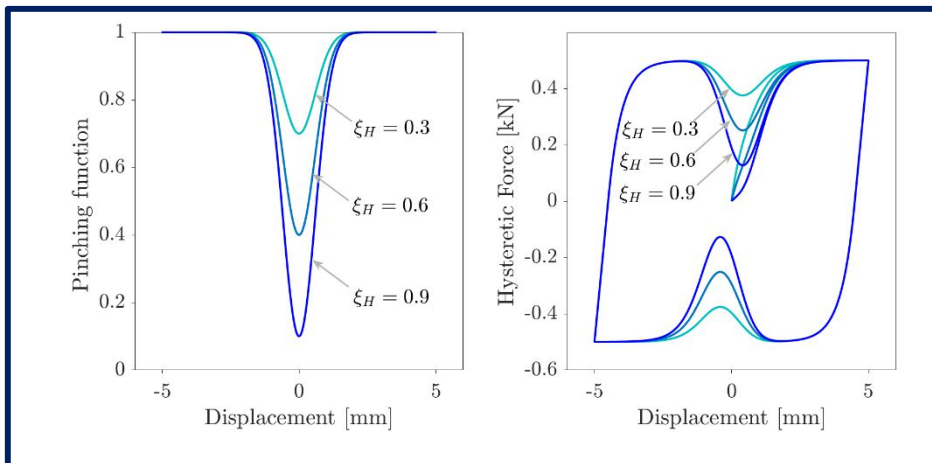
where $x_0 \in R^+$, $\xi_0 \in [0, 1)$

Extension

Intensity

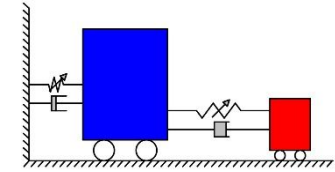


Biagio Carboni, Walter Lacarbonara, and Ferdinando Auricchio.
Journal of Engineering Mechanics 141.3 (2014): 04014135.





Nonlinear Structural Identification



- Structural parameters to be identified: $\theta = \{k_{e1}, k_{d1}, \gamma_1, \beta_1, n_1\}$
 - Analytical Optimization
- (n = 1)

$$\begin{aligned} \bar{f}_{ul} &= \frac{1}{2} \sqrt{\frac{k_{e1}}{m_1}} = 4.23 \text{ Hz} \rightarrow \bar{k}_{e1} = 0.3610 \text{ kN/mm} \\ \bar{f}_{in} &= \frac{1}{2} \sqrt{\frac{k_{e1} + k_{d1}}{m_1}} = 4.02 \text{ Hz} \rightarrow \bar{k}_{d1} = 0.0387 \text{ kN/mm} \\ \bar{f}_{95} &= \frac{1}{2} \sqrt{\frac{k_{e1} + 0.317 \bar{k}_{ed}}{m_1}} = 4.0875 \text{ Hz} \rightarrow \bar{x}_{95} \cong 10 \text{ mm} \\ \bar{x}_{95} &= \frac{3}{\bar{\gamma}_1 + \bar{\beta}_1} \rightarrow \bar{\gamma}_1 + \bar{\beta}_1 = 0.30 \text{ mm}^{-1} \end{aligned}$$

- Numerical Optimization: **Differential Evolution Algorithms**

R Storn and K Price, *Journal of global optimization*, vol. 11, no. 4, pp. 341–359, 1997.

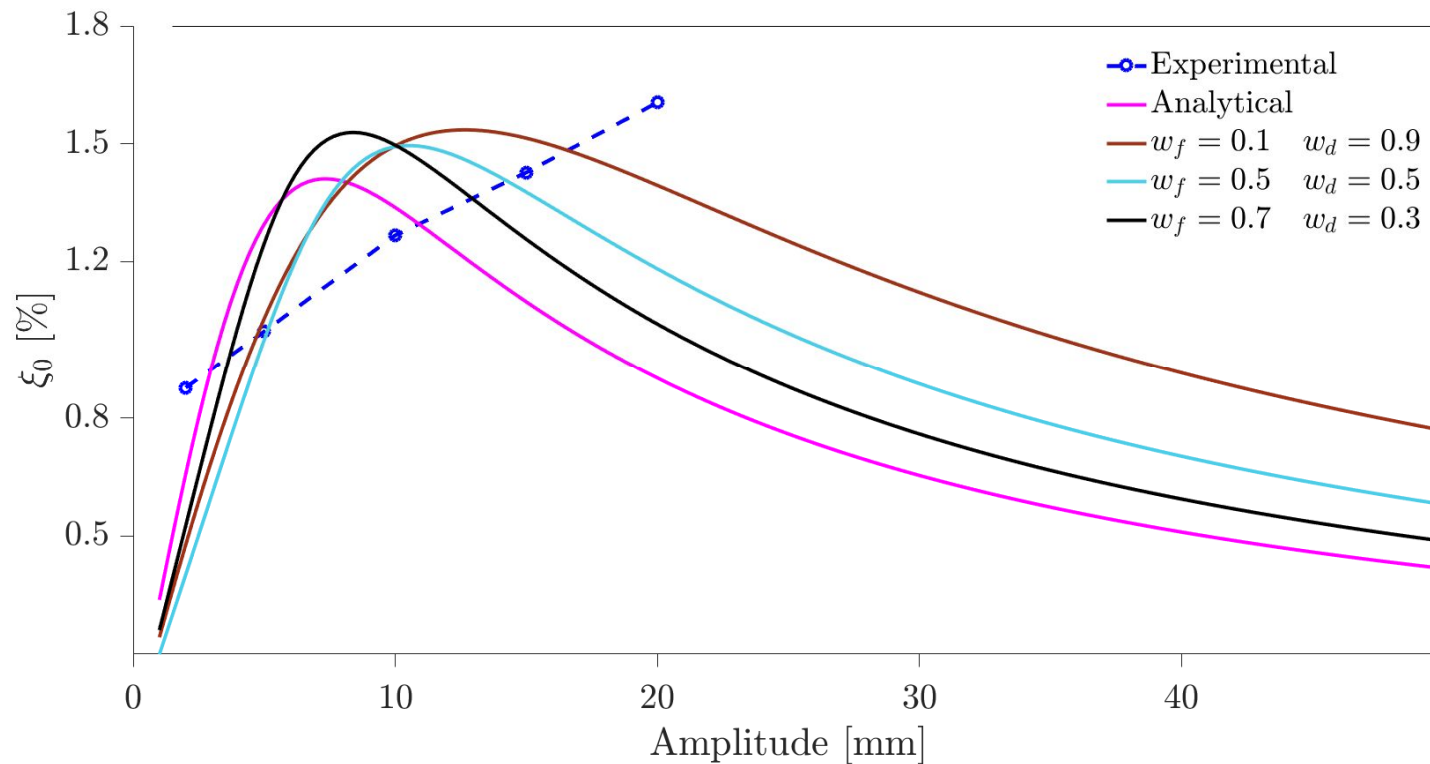
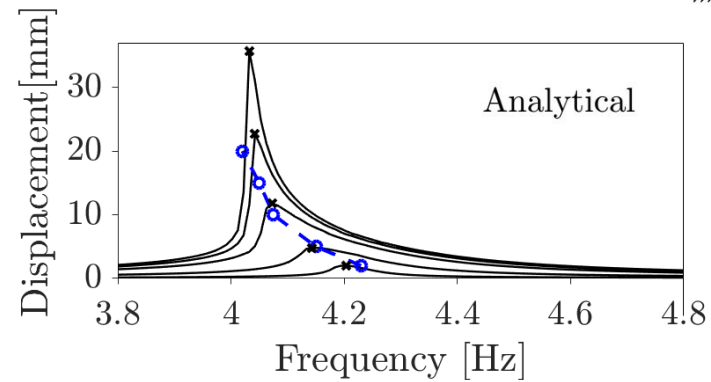
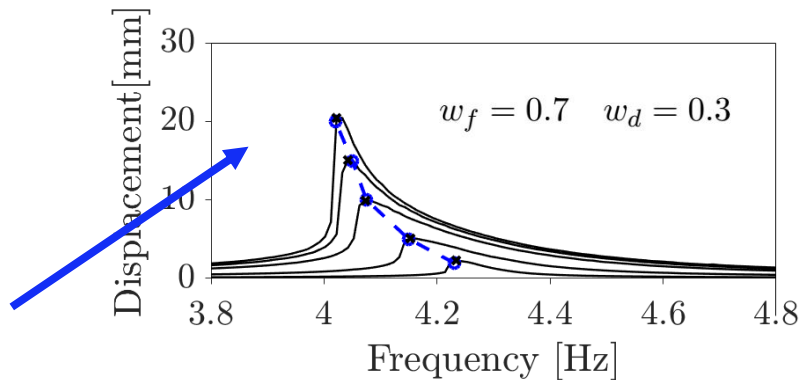
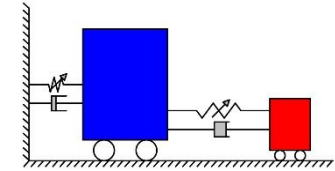
Cost function:

$$\Phi_{id}(\theta) = \sum_{i=1}^M w_f \frac{(f_{ex,i} - f_{m,i}(\theta))}{f_{ex,i}} + w_\xi \frac{(\xi_{ex,i} - \xi_{m,i}(\theta))}{\xi_{ex,i}}$$

Resonant frequency		Damping		Weight function	
f_{ex}	Experimental	ξ_{ex}	Experimental	w_f	Frequency
f_m	Estimated frequency	ξ_m	Estimated	w_ξ	Damping

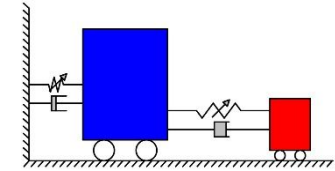


Nonlinear Structural Identification





Optimum design of the hysteretic TMD



- TMD parameters to be optimized:

$$\mathbf{d} = \{k_{e2}, k_{d2}, k_{c2}, \gamma_2, \beta_2, n_2, m_2, \xi_H, x_H\}$$

- Optimization method: **Differential Evolution Algorithms**

$$n_2 = 1$$

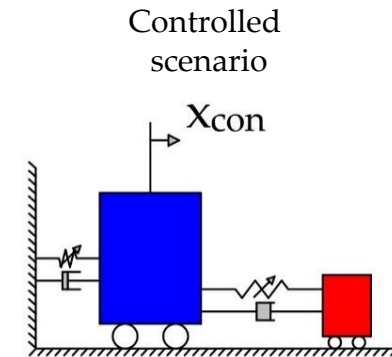
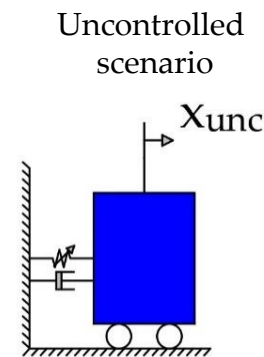
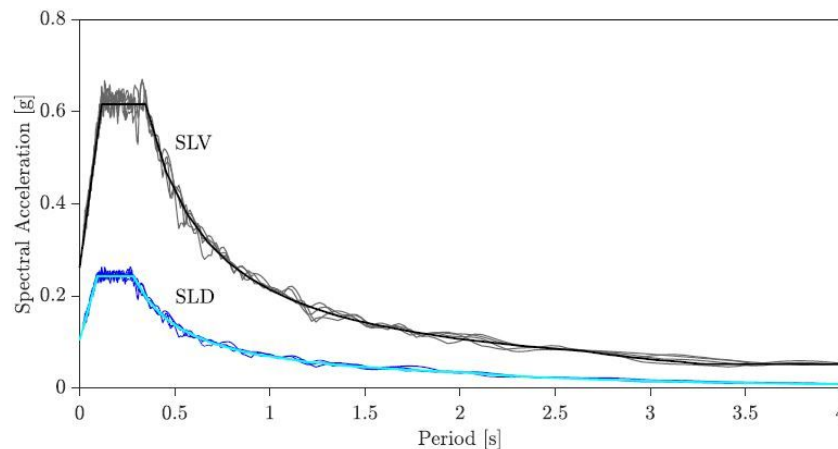
$$\mu = \frac{m_2}{m_1} = \{1\%, 2\%, 5\%\}$$

Cost function:

$$R_t(\mathbf{d}) = 1 - \Psi_t(\mathbf{d})$$

Input

4 SLD + 4 SLV

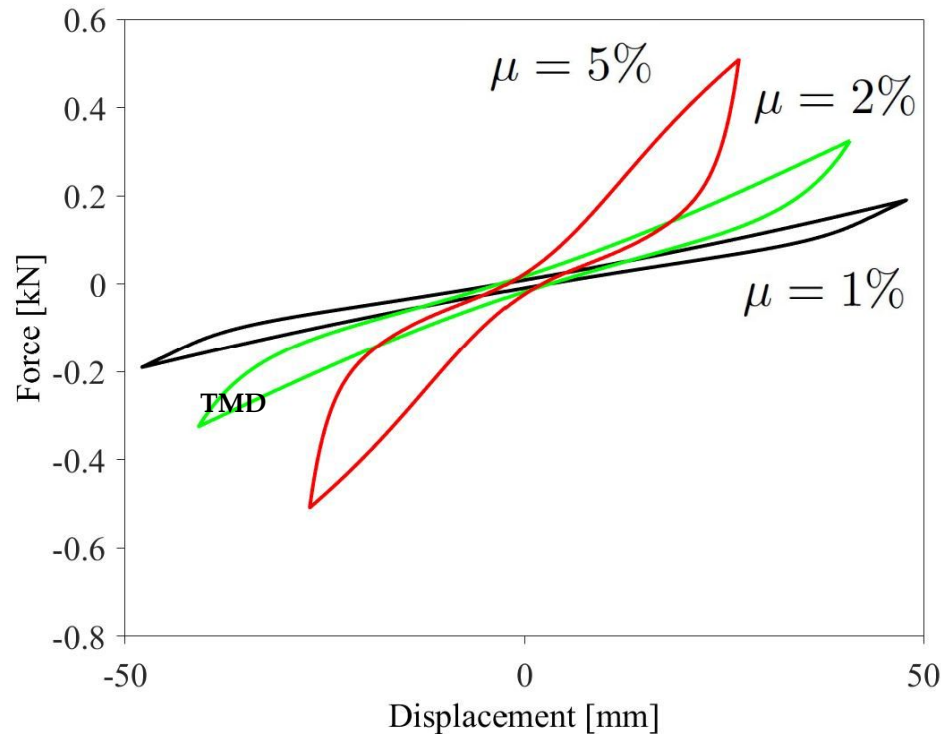


k_{d2} [$\frac{\text{kN}}{\text{mm}}$]	k_{c2} [$\frac{\text{kN}}{\text{mm}^3}$]	γ_2 [$\frac{\text{kN}^{1-n_1}}{\text{mm}}$]	β_2 [$\frac{\text{kN}^{1-n_1}}{\text{mm}}$]	ξ_H [-]	x_H [mm^2]
$\frac{k_{e1}}{1000}$	0	$\frac{\gamma_1}{1000}$	$\frac{\beta_1}{1000}$	0	20
$30k_{e1}$	k_{e1}	$100\gamma_1$	$100\beta_1$	0.985	40000

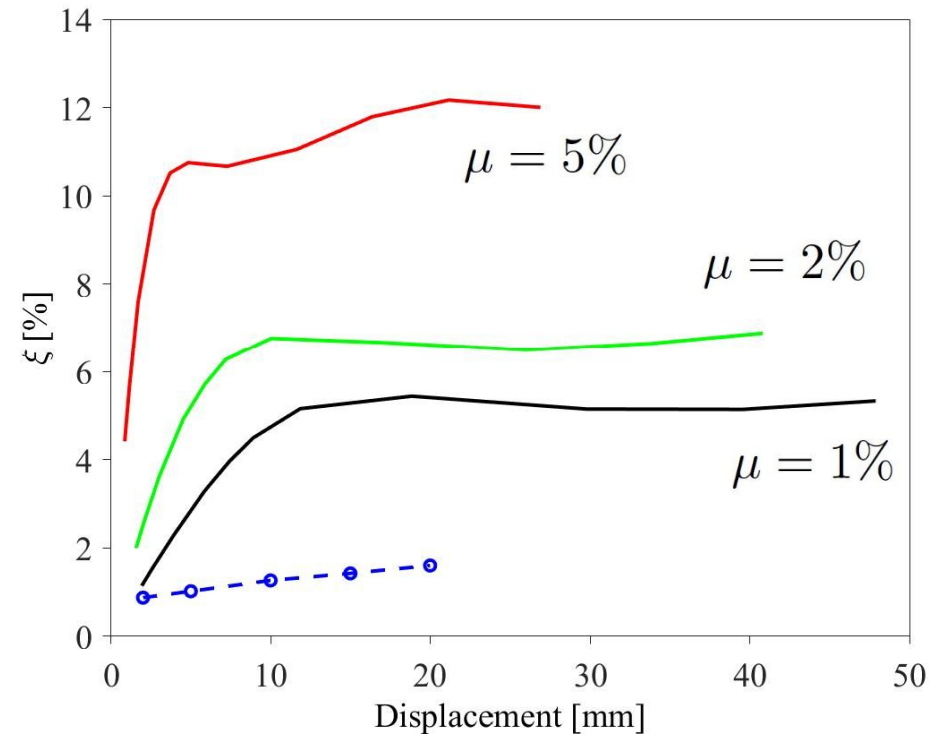


Optimized hysteretic TMD

Force-Displacement Cycles



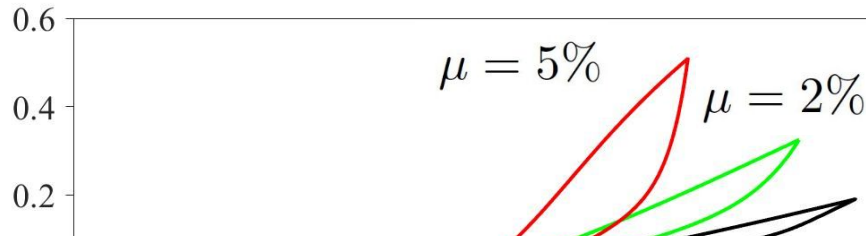
Dampings



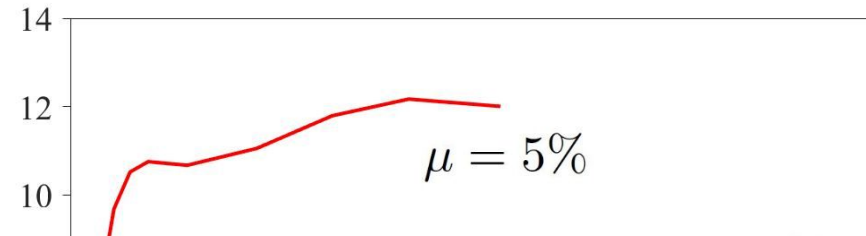


Optimized hysteretic TMD

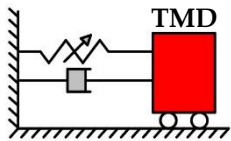
Force-Displacement Cycles



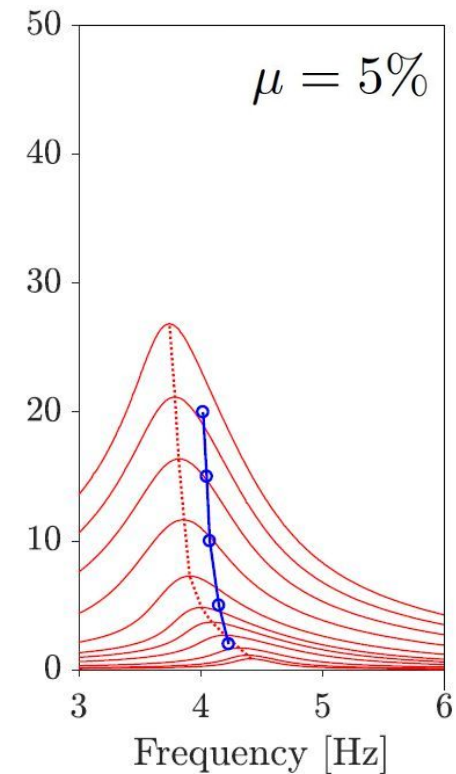
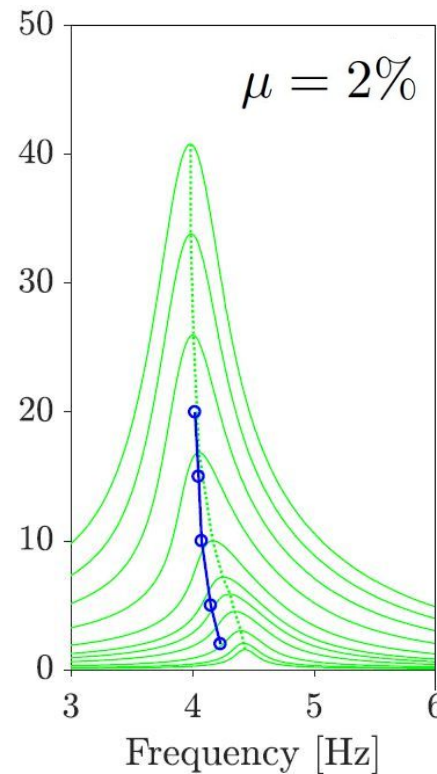
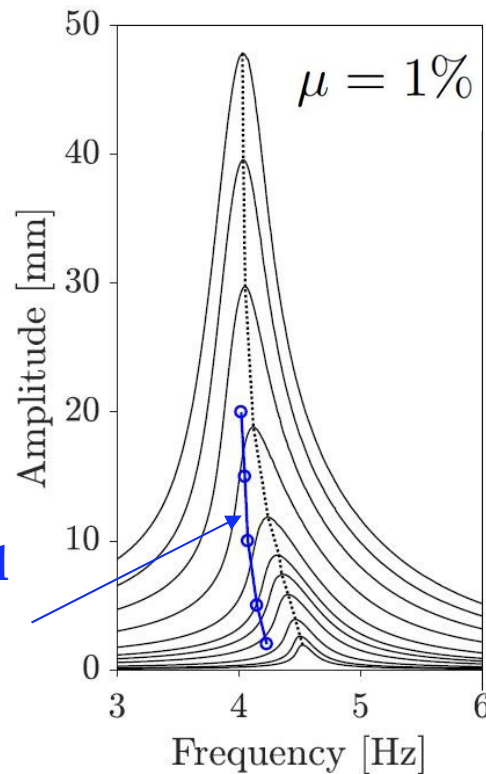
Dampings



FRCs 1DOF



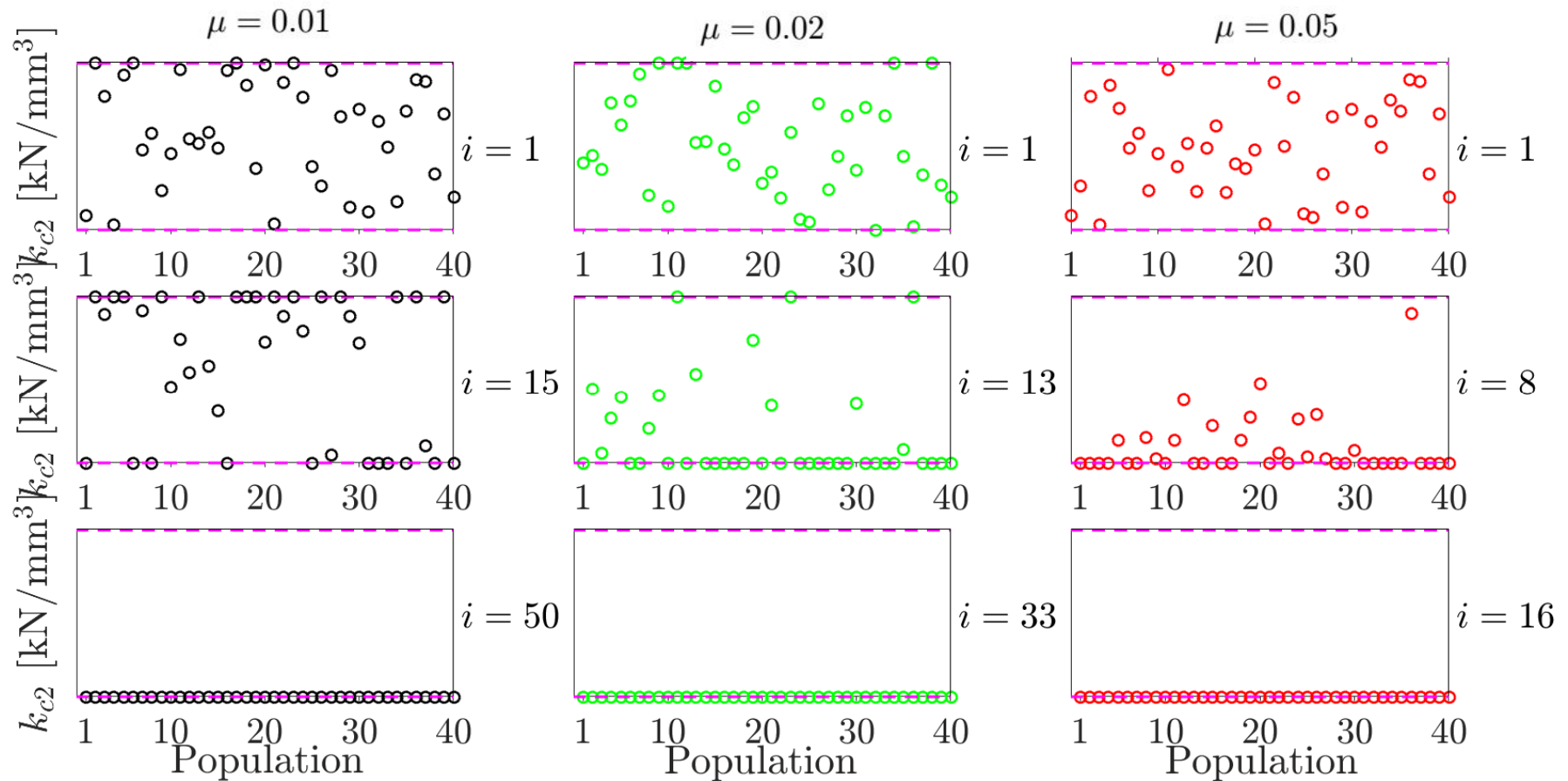
Experimental
structural
Backbone





Optimized hysteretic TMD

Effect of the cubic elastic stiffness

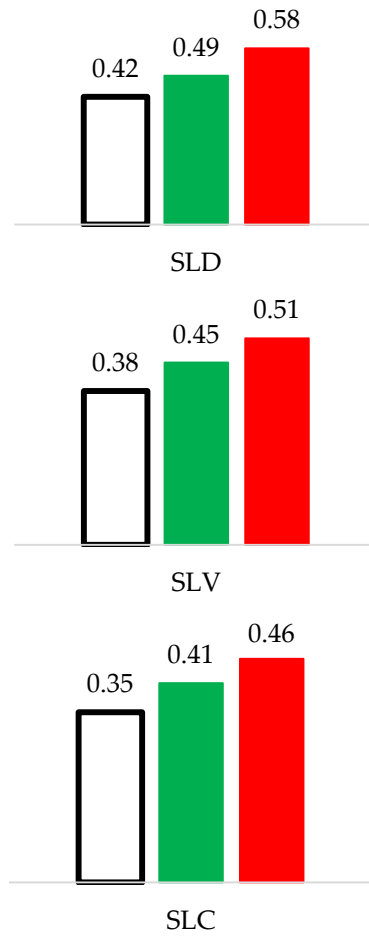


Not needed!

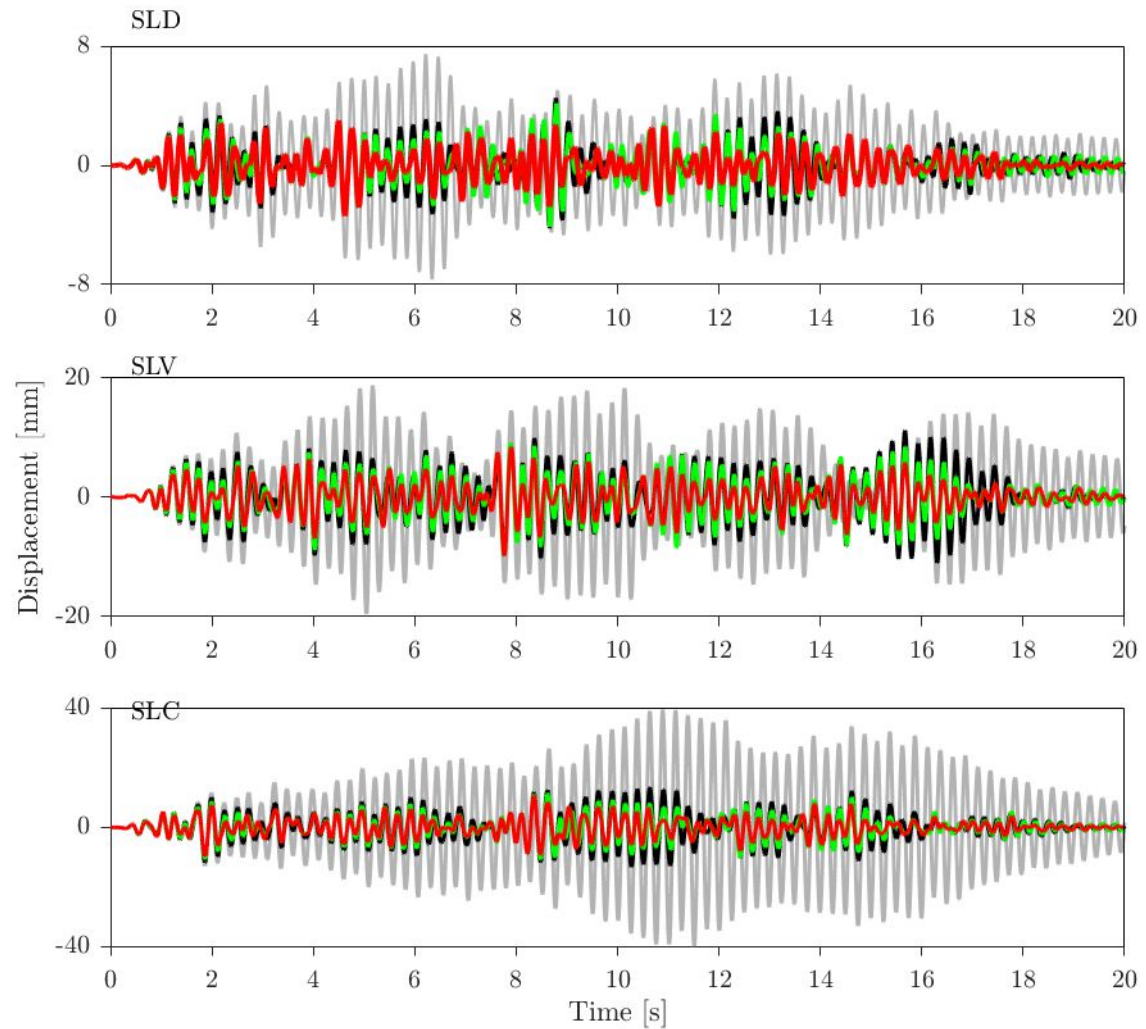


Optimized hysteretic TMD: mitigation capability

Objective function
Rt for each limit state



Displacement reductions



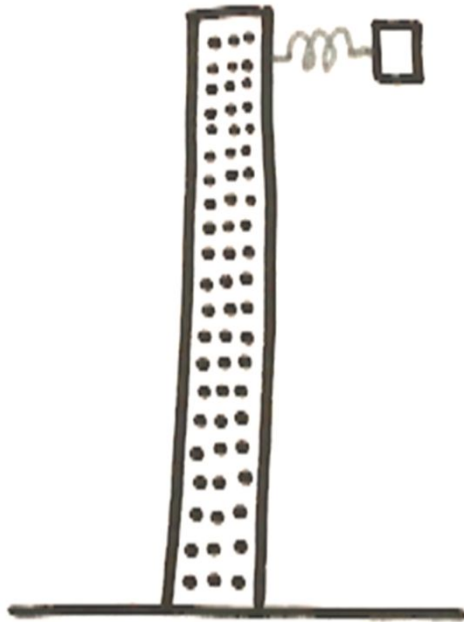


Main achievements:

- ✓ Novel **identification** technique for nonlinear structures and **optimization** of TMD parameters based on **Differential Evolution** are proposed.
- ✓ **Design formulas** were obtained in order to identify the hysteretic structures.
- ✓ Improvement in the RMS displacement mitigation: over **40%** for **steel-made** structures, were obtained using hysteretic TMD endowed with a mass corresponding to **1%** of the mass of the structure.
- ✓ The optimized force-displacement cycles showed a **pronounced pinching shape**.
- ✓ The pinched hysteretic TMD is effective in protecting a nonlinear hysteretic structure thanks to its **softening-type backbone**, which can be optimized to **accommodate the frequency changes** that the engineering structures undergo when subject to seismic events.



Hysteretic Tuned Mass Dampers for Seismic Protection



**Thank you
for your attention**

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May 20, 2021